

# Supporting Data-Driven Mathematics

Online databases made easy  
(for simple datasets)

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# Some Famous Online Combinatorial Math Databases

lmfdb.org

findstat.org

oeis.org



# The Other 80% (or more)

[N]J	V	E	T <sub>1</sub>	W <sup>2</sup>	DT	IAGI
C4.5.1.1	5	10	DT	W	NB	120
C4.6.1.1	6	12	DT	U	NB	48
C4.8.1.1	8	16	DT	U	Bip	(2*7)(3*2)
C4.9.1.1	9	18	DT	W	NB	72
C4.10.1.1	10	20	DT	U	NB	320
C4.10.2.1	10	20	DT	W	Bip	240
C4.12.1.1	12	24	DT	U	Bip	768
C4.12.2.1	12	24	DT	W	NB	48
C4.13.1.1	13	26	DT	W	NB	52
C4.14.1.1	14	28	DT	U	NB	(2*8)(7*1)
C4.14.2.1	14	28	DT	W	Bip	336
C4.15.1.1	15	30	DT	W	NB	60
C4.15.2.1	15	30	DT	W	NB	120
C4.16.1.1	16	32	DT	U	Bip	(2*12)
C4.16.2.1	16	32	DT	W	Bip	384
C4.17.1.1	17	34	DT	W	NB	68
C4.18.1.1	18	36	DT	U	NB	(2*10)(3*2)
C4.18.2.1	18	36	DT	W	Bip	144
C4.20.1.1	20	40	DT	U	Bip	(2*12)(5*1)
C4.20.2.1	20	40	DT	W	Bip	80
C4.20.3.1	20	40	DT	W	NB	320
C4.20.4.1	20	40	SS	U	Bip	(2*8)(3*1)(5*1)
C4.21.1.1	21	42	DT	W	NB	84
C4.21.2.1	21	42	DT	W	NB	336

- Graphs of order 4 to 300 (18 MB)
- Graphs of order 302 to 500 (66 MB)
- Graphs of order 502 to 600 (69 MB)
- Graphs of order 602 to 700 (84 MB)
- Graphs of order 702 to 800 (114 MB)
- Graphs of order 802 to 900 (147 MB)
- Graphs of order 902 to 1000 (183 MB)
- Graphs of order 1002 to 1050 (164 MB)
- Graphs of order 1052 to 1100 (113 MB)
- Graphs of order 1102 to 1150 (103 MB)
- Graphs of order 1152 to 1200 (234 MB)
- Graphs of order 1202 to 1250 (137 MB)
- Graphs of order 1252 to 1280 (131 MB)

Potočnik, Spiga, Verret; A census of small connected cubic vertex-transitive graphs

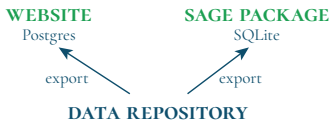
```

cubvtr[1] := 1..4 in {1,2,3,4};
cubvtr[1,1] := Graphs [ (1,2), (1,3), (2,3), (1,2), (1,3), (1,4), (2,4) ];
cubvtr[1,2] := Graphs [ (1,2), (1,3), (2,3), (1,4), (1,3), (1,4), (2,3), (1,4), (2,3) ];
cubvtr[1,3] := Graphs [ (1,2), (1,3), (2,3), (1,4), (1,3), (1,4), (2,3), (1,4), (2,3) ];
cubvtr[1,4] := Graphs [ (1,2), (1,3), (2,3), (1,4), (1,3), (1,4), (2,3), (1,4), (2,3) ];
cubvtr[1,5] := Graphs [ (1,2), (1,3), (2,3), (1,4), (1,3), (1,4), (2,3), (1,4), (2,3) ];
cubvtr[1,6] := Graphs [ (1,2), (1,3), (2,3), (1,4), (1,3), (1,4), (2,3), (1,4), (2,3) ];
cubvtr[1,7] := Graphs [ (1,2), (1,3), (2,3), (1,4), (1,3), (1,4), (2,3), (1,4), (2,3) ];
cubvtr[1,8] := Graphs [ (1,2), (1,3), (2,3), (1,4), (1,3), (1,4), (2,3), (1,4), (2,3) ];
cubvtr[1,9] := Graphs [ (1,2), (1,3), (2,3), (1,4), (1,3), (1,4), (2,3), (1,4), (2,3) ];
cubvtr[1,10] := Graphs [ (1,2), (1,3), (2,3), (1,4), (1,3), (1,4), (2,3), (1,4), (2,3) ];
cubvtr[1,11] := Graphs [ (1,2), (1,3), (2,3), (1,4), (1,3), (1,4), (2,3), (1,4), (2,3) ];
cubvtr[1,12] := Graphs [ (1,2), (1,3), (2,3), (1,4), (1,3), (1,4), (2,3), (1,4), (2,3) ];
cubvtr[1,13] := Graphs [ (1,2), (1,3), (2,3), (1,4), (1,3), (1,4), (2,3), (1,4), (2,3) ];
cubvtr[1,14] := Graphs [ (1,2), (1,3), (2,3), (1,4), (1,3), (1,4), (2,3), (1,4), (2,3) ];
cubvtr[1,15] := Graphs [ (1,2), (1,3), (2,3), (1,4), (1,3), (1,4), (2,3), (1,4), (2,3) ];
cubvtr[1,16] := Graphs [ (1,2), (1,3), (2,3), (1,4), (1,3), (1,4), (2,3), (1,4), (2,3) ];
cubvtr[1,17] := Graphs [ (1,2), (1,3), (2,3), (1,4), (1,3), (1,4), (2,3), (1,4), (2,3) ];
cubvtr[1,18] := Graphs [ (1,2), (1,3), (2,3), (1,4), (1,3), (1,4), (2,3), (1,4), (2,3) ];
cubvtr[1,19] := Graphs [ (1,2), (1,3), (2,3), (1,4), (1,3), (1,4), (2,3), (1,4), (2,3) ];
cubvtr[1,20] := Graphs [ (1,2), (1,3), (2,3), (1,4), (1,3), (1,4), (2,3), (1,4), (2,3) ];
cubvtr[1,21] := Graphs [ (1,2), (1,3), (2,3), (1,4), (1,3), (1,4), (2,3), (1,4), (2,3) ];
cubvtr[1,22] := Graphs [ (1,2), (1,3), (2,3), (1,4), (1,3), (1,4), (2,3), (1,4), (2,3) ];
cubvtr[1,23] := Graphs [ (1,2), (1,3), (2,3), (1,4), (1,3), (1,4), (2,3), (1,4), (2,3) ];
cubvtr[1,24] := Graphs [ (1,2), (1,3), (2,3), (1,4), (1,3), (1,4), (2,3), (1,4), (2,3) ];
cubvtr[1,25] := Graphs [ (1,2), (1,3), (2,3), (1,4), (1,3), (1,4), (2,3), (1,4), (2,3) ];
cubvtr[1,26] := Graphs [ (1,2), (1,3), (2,3), (1,4), (1,3), (1,4), (2,3), (1,4), (2,3) ];
cubvtr[1,27] := Graphs [ (1,2), (1,3), (2,3), (1,4), (1,3), (1,4), (2,3), (1,4), (2,3) ];
cubvtr[1,28] := Graphs [ (1,2), (1,3), (2,3), (1,4), (1,3), (1,4), (2,3), (1,4), (2,3) ];
cubvtr[1,29] := Graphs [ (1,2), (1,3), (2,3), (1,4), (1,3), (1,4), (2,3), (1,4), (2,3) ];
cubvtr[1,30] := Graphs [ (1,2), (1,3), (2,3), (1,4), (1,3), (1,4), (2,3), (1,4), (2,3) ];
    
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Wilson, Potočnik; A Census of edge-transitive tetravalent graphs



# Beginnings



Janoš Vidali




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## Janoš's SageMath package

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Compare objects (both ways!)
sage: G = CVTGraph(10, 3)
sage: G.is_isomorphic(graphs.PetersenGraph())
True
  
```

Use the object `info` to query the database

```

sage: gen = info.all(is_partial_cube, orderby=order) # sort by num. of vcs.
sage: next(gen) # first matching graph
3-Cube: cubic vertex-transitive graph on 8 vertices, number 2
sage: next(gen) # second matching graph
6-Prism: cubic vertex-transitive graph on 12 vertices, number 3

sage: info.count(cvt_index) # number of graphs in the CVT census
111360
sage: info.count(cvt_index, groupby=girth) # break down by girth
{3: 160, 4: 5754, 5: 100, 6: 58674, 7: 192, 8: 13529, 9: 219,
10: 25806, 11: 80, 12: 5423, 13: 37, 14: 1365, 15: 12, 16: 9}
  
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## Search

Graphs  Maniplexes

- vertex transitive graphs
- cubic vertex transitive graphs
- cubic arc transitive graphs

Matches found: 4

Display results

Choose columns

order	CVT	diameter	girth	is arc transitive	is cayley	is hamiltonian
20	7	5	6	true	false	true
24	11	6	4	false	true	true
48	29	9	4	false	true	true
120	60	15	4	false	true	true

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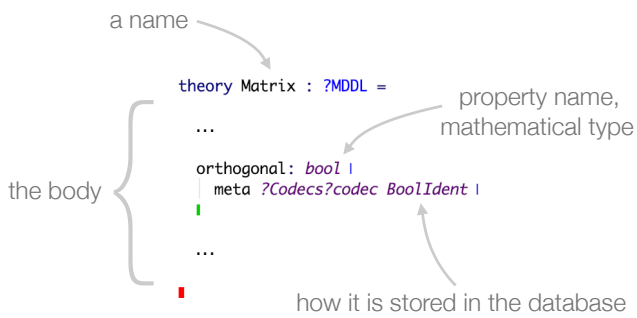
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## Anatomy of a schema theory



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## Take-away points

If you would like to use this project for your data, please contact me!

**[katja.bercic@fau.de](mailto:katja.bercic@fau.de)**

You can also help with gathering information about math datasets:

**[mathdb.mathhub.info](http://mathdb.mathhub.info)**



A big thanks goes to OpenDreamKit. It made the existence of this project possible and gave it a big boost.

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```
namespace http://data.mathhub.info/schemas |  
  
theory MatrixS : ?MDDL =  
  meta ?MDDL?schemaGroup "Joe" |  
  
  mat: matrix int 2 2 |  
  | meta ?Codecs?codec MatrixAsArray IntIdent |  
  | tag ?MDDL?opaque |  
  |  
  
  trace: int |  
  | meta ?Codecs?codec IntIdent |  
  |  
  
  orthogonal: bool |  
  | meta ?Codecs?codec BoolIdent |  
  |  
  
  eigenvalues: list int |  
  | meta ?Codecs?codec ListAsArray IntIdent |  
  | tag ?MDDL?opaque |  
  |
```

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